# The Crystal Structure of Cadmium Diborate, $\mathbf{C d O} . \mathbf{2 B}_{2} \mathrm{O}_{\mathbf{3}}$ 

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#### Abstract

The crystal structure of cadmium diborate has been determined by a three-dimensional Fourier synthesis. The atomic position parameters have been refined by a least-squares analysis including 519 reciprocal-lattice points. A residual index $R$ equal to $8.5 \%$ was obtained. The structure consists of two interlocking, identical networks. The networks are built up from a single type of borate unit, composed of four borate polyhedra. A boron-oxygen arrangement of this type has first been found in the isolated polyanion unit of borax. $50 \%$ of the boron atoms are fourfold coordinated in the structure. The cadmium atoms are surrounded by four close oxygens, arranged in a distorted tetrahedron.


## Introduction

The structures of several compounds with a ratio of metal oxide to boron oxide of 1 to 2 are known. The hydrated compounds $\mathrm{Na}_{2} \mathrm{O} \cdot 2 \mathrm{~B}_{2} \mathrm{O}_{3} \cdot 10 \mathrm{H}_{2} \mathrm{O}$ (Morimoto, 1956) and $\mathrm{K}_{2} \mathrm{O} \cdot 2 \mathrm{~B}_{2} \mathrm{O}_{3} \cdot 4 \mathrm{H}_{2} \mathrm{O}$ (Marezio, Plettinger \& Zachariasen, 1963) contain a characteristic double ring polyion as an isolated unit. In the anhydrous lithium diborate, $\mathrm{Li}_{2} \mathrm{O} .2 \mathrm{~B}_{2} \mathrm{O}_{3}$, these double ring polyions are condensed to two interlocking threedimensional networks (Krogh-Moe, 1962). $50 \%$ of the boron atoms are fourfold coordinated in all these phases, conforming to the rule that the number of borons in fourfold coordination is equal to the total number of charge units carried by foreign cations (excluding $\mathrm{H}^{+}$).

Recently the structure of strontium diborate, SrO . $2 \mathrm{~B}_{2} \mathrm{O}_{3}$, has been determined (Krogh-Moe, 1964). Here a completely different type of network is found, having all the boron atoms in fourfold coordination. As a consequence some of the oxygen atoms are coordinated by three boron atoms. This is contrary to prevailing ideas about oxygen always acting as a bridge between two network-forming cations in the so called network structures. An inquiry into the condition for abnormal coordination numbers of oxygen is thus of some interest.

The difference in coordination behaviour of the lithium and strontium diborates obviously must originate in properties of the cation. Simple empirical correlations between boron coordination behaviour and parameters of the cation, such as radius, charge, electronegativity or polarizability are conceivable. On the other hand the dependence of boron coordination on the cation could also be of a more complex nature. To elucidate this question, structural data about other diborates are highly desirable, and an investigation of the structure of cadmium diborate was therefore undertaken.

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## Experimental

Crystalline cadmium diborate was prepared by fusing boric acid with a small excess of cadmium oxide, and annealing the supercooled melt at $800^{\circ} \mathrm{C}$.
Unit-cell dimensions for cadmium diborate have previously been given by Hand \& Krogh-Moe (1962). For the present work the unit-cell dimensions were refined by a least-squares adjustment, using nine indexed powder lines from a diffractometer recording. The following dimensions were found:
$a=8.21 \pm 0.01, \quad b=8.70 \pm 0.01, \quad c=14.18 \pm 0.02 \AA$
Space group Pbca. The calculated and observed densities with 8 formula units in the unit cell are 3.51 and $3.52 \mathrm{~g} . \mathrm{cm}^{-3}$ respectively.
A single crystal of the sample was ground to a nearly perfect sphere of radius $R=0.005 \mathrm{~cm}$. With Mo $K \alpha-$ radiation the linear absorption coefficient is $44 \mathrm{~cm}^{-1}$, making absorption errors quite small for a sphere of this size ( $\mu R=0 \cdot 22$ ).
Integrated multiple-film Weissenberg exposures were obtained for the zero to seventh layers, rotating the crystal around the $a$ axis and using Mo $K \alpha$-radiation. The intensities were measured photometrically in 519 points in the reciprocal lattice and corrected for the Lorentz and polarization factors in the usual manner.

## Determination of the structure

The unit cell contains 8 cadmium atoms, occupying, as it turns out, a single general position. The three positional parameters of the cadmium atom were determined from Patterson projections along two of the axes. Signs derived from this heavy atom position together with the experimental structure factors were employed for calculating a complete three-dimensional Fourier synthesis. From the electron density sections thus obtained, a crude model of the structure was constructed settling the positions of the 4 boron and 7 oxygen atoms of the asymmetric unit. The structure was subsequently refined by the method of least squares,
using the program written by S．Aleby for the SAAB D21 computer of the crystallographic group at the In－ situte of Medical Biochemistry in Göteborg．A final reliability index of $R=8.5 \%$ was obtained．

A list of final positional parameters and temperature factors，together with standard deviations，is given in Table 1．Table 2 gives the observed and calculated structure factors．

## Description and discussion of the structure

The structure consists of two infinite three－dimensional networks of boron－oxygen linkages．This is shown in

Fig．1，which gives a projection of the structure along the $a$ axis．The connexions of the networks perpen－ dicular to the plane of the paper are easily recognized by considering the operation of the twofold screw axes normal to the paper plane．（These screw axes have the following $y, z$ values： $\left.0, \frac{1}{4} ; 0, \frac{3}{4} ; \frac{1}{2}, \frac{1}{4} ; \frac{1}{2}, \frac{3}{4}\right)$ ．

Each of the twin networks can be derived from the other by the symmetry operations of the space group， and is thus separate and interlocking．（For clarity one of the networks is shown dashed in Fig．1．）This phen－ omenon of two interlocking，but separate，borate net－ works has been found in several other anhydrous bor－ ate structures（Krogh－Moe，1962，1965）．

Table 1．Atomic position parameters，with standard deviations
Values are given as fractions multiplied by $10^{4}$ ，of the unit cell edge．The last two columns give the parameter $B$（together with its standard deviation）of the temperature factor $\exp \left[-B(\sin \theta / \lambda)^{2}\right]$ ．Temperature factors of atoms $O(4), O(5), B(3)$ and $B(4)$ were arbitrarily fixed at $0 \cdot 1$ to avoid（small）negative values during refinement．

| Atom | $x / a$ | $\sigma_{x / a}$ | $y / b$ | $\sigma_{y / b}$ | $z / c$ | $\sigma_{z / c}$ | $B$ | $\sigma_{B}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Cd | 1210 | 2 | 1105 | 2 | 1125 | 1 | $0 \cdot 94 \AA^{2}$ | $0 \cdot 02$ |
| $\mathrm{O}(1)$ | 543 | 17 | 4103 | 17 | 1875 | 10 | $0 \cdot 58$ | $0 \cdot 03$ |
| $\mathrm{O}(2)$ | 3853 | 15 | 1325 | 13 | 980 | 8 | $0 \cdot 40$ | $0 \cdot 03$ |
| $\mathrm{O}(3)$ | 3544 | 22 | 3759 | 17 | 21 | 9 | $1 \cdot 18$ | $0 \cdot 03$ |
| $\mathrm{O}(4)$ | 4733 | 14 | 3837 | 15 | 1489 | 8 | $0 \cdot 10$ | - |
| $\mathrm{C}(5)$ | 5335 | 17 | 1642 | 16 | 2433 | 8 | $0 \cdot 10$ | - |
| $\mathrm{O}(6)$ | 6094 | 18 | 2561 | 19 | 201 | 10 | $0 \cdot 94$ | $0 \cdot 03$ |
| $\mathrm{O}(7)$ | 6595 | 16 | 428 | 17 | 1147 | 10 | $0 \cdot 94$ | $0 \cdot 02$ |
| $\mathrm{~B}(1)$ | 4473 | 28 | 2864 | 30 | 679 | 18 | $1 \cdot 04$ | $0 \cdot 04$ |
| $\mathrm{~B}(2)$ | 5140 | 27 | 3285 | 26 | 2346 | 15 | $0 \cdot 44$ | $0 \cdot 03$ |
| $\mathrm{~B}(3)$ | 5061 | 23 | 640 | 23 | 1624 | 14 | $0 \cdot 10$ | - |
| $\mathrm{B}(4)$ | 7019 | 25 | 1374 | 22 | 425 | 14 | $0 \cdot 10$ | - |

Table 2．Observed and calculated structure factors
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| 1 | 8 |
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| 1 | 9 |
| 1 | 10 |
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| 2 | 9 |
| 2 |  |


 NNNテNNNmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmmm





 WWWWNNNNNNNNRースースースー－






It is apparent from Fig. 1 that the network may be described as composed of borate units having 4 boron atoms and 5 oxygen atoms within the unit as well as 4 oxygen atoms shared with 4 adjacent units. This double ring structure was first discovered as the isolated polyion, $\mathrm{B}_{4} \mathrm{O}_{5}(\mathrm{OH})_{4}^{2-}$, in the mineral borax by Morimoto (1956). Later, the group was found as part of a network structure in $\mathrm{Li}_{2} \mathrm{O} .2 \mathrm{~B}_{2} \mathrm{O}_{3}$ (Krogh-Moe, 1962). The twin networks in the lithium compound are arranged somewhat differently from those reported here, however.

Interatomic bond distances are given in Table 3. The average of the boron-oxygen bond distances in the $\mathrm{BO}_{4}$ tetrahedra is $1.47 \AA$ as opposed to $1.37 \AA$ for the $\mathrm{BO}_{3}$ triangles. This compares well with the corresponding mean bond lengths observed in potassium diborate tetrahydrate, viz. $1.480 \AA$ and $1.368 \AA$ for tetrahedra and triangles respectively (Marezio, Plettinger \& Zachariasen, 1963). What appear to be significant variations from the average values in the individual bond lengths (up to 6 times the standard deviation of 0.008 $\AA$ ) were found by these authors. The boron-oxygen bond lengths obtained by us [excepting the $\mathrm{B}(2)-\mathrm{O}(5)$ distance] vary within 3 times the standard deviations of $0.02 \AA$, and too much emphasis should therefore not be placed on these variations. A real effect as large as that obtained would not be unexpected, however.

The cation coordination is noteworthy. Cadmium is surrounded by four close oxygen atoms at distances $2 \cdot 18,2 \cdot 19,2 \cdot 21$ and $2 \cdot 22 \pm 0 \cdot 01 \AA$. Then follow oxygen


Fig. 1. A projection of the structure along the $a$ axis, showing how the structural units are interlinked to a three-dimensional network. Black circles: boron; open circles: oxygen; large open circles: cadmium. The network indicated by dashed lines is a separate interlocking twin of the first network. The unit-cell dimensions are indicated by the rectangle.

Table 3. Interatomic distances
Boron-oxygen bond lengths (standard deviation $\pm 0.02 \AA$ ) of the boron coordination polyhedra.
Tetrahedra

| $\mathrm{B}(1)-\mathrm{O}(2)$ | $1.50 \AA$ | $\mathrm{~B}(3)-\mathrm{O}(1)$ | $1.47 \AA$ |
| :---: | :--- | :--- | :--- |
| $\mathrm{~B}(1)-\mathrm{O}(3)$ | 1.43 | $\mathrm{~B}(3)-\mathrm{O}(2)$ | 1.47 |
| $\mathrm{~B}(1)-\mathrm{O}(4)$ | 1.44 | $\mathrm{~B}(3)-\mathrm{O}(5)$ | 1.46 |
| $\mathrm{~B}(1)-\mathrm{O}(6)$ | 1.52 | $\mathrm{~B}(3)-\mathrm{O}(7)$ | 1.44 |
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| gles |  |  |  |
| $\mathrm{B}(2)-\mathrm{O}(1)$ | $1.35 \AA$ | $\mathrm{~B}(4)-\mathrm{O}(3)$ | 1.41 |
| $\mathrm{~B}(2)-\mathrm{O}(4)$ | 1.35 | $\mathrm{~B}(4)-\mathrm{O}(6)$ | 1.32 |
| $\mathrm{~B}(2)-\mathrm{O}(5)$ | 1.45 | $\mathrm{~B}(4)-\mathrm{O}(7)$ | 1.36 |

Cadmium-oxygen distances (standard deviation $\pm 0.01 \AA$ )

| $\mathrm{Cd}-\mathrm{O}(4)$ | $2.18 \AA$ |
| :--- | :--- |
| $\mathrm{Cd}-\mathrm{O}(2)$ | 2.19 |
| $\mathrm{Cd}-\mathrm{O}(6)$ | 2.21 |
| $\mathrm{Cd}-\mathrm{O}(5)$ | 2.22 |
| $\mathrm{Cd}-\mathrm{O}(3)$ | 2.58 |
| $\mathrm{Cd}-\mathrm{O}(31)$ | 2.73 |
| $\mathrm{Cd}-\mathrm{O}(1)$ | 2.87 |

atoms at $2.59 \AA$ and farther away (cf. Table 3). The four close oxygen atoms are arranged in a distorted tetrahedron. (The six $\mathrm{O}-\mathrm{Cd}-\mathrm{O}$ angles of this coordination polyhedron are $81 \cdot 9,85 \cdot 2,112 \cdot 9,116 \cdot 9,131 \cdot 1$ and $131 \cdot 4 \pm 0 \cdot 6^{\circ}$.) The bond distance within the tetrahedron is closer to that obtained from the tetrahedral covalent radii of cadmium and oxygen, i.e. $2 \cdot 14 \AA$, than to the bond distance, $2 \cdot 37 \AA$, calculated from the (octahedral) ionic radii (Pauling, 1960). The cadmium atom therefore seems to be essentially covalent tetrahedrally bonded, though other oxygens probably take some smaller part in the bonding.

The cadmium diborate and the lithium diborate are both characterized by a somewhat shorter metal-oxygen bond than found in the strontium compound. It is still imprudent to single out a short metal-oxygen bond as a decisive factor in the formation of the 'normal' $\mathrm{B}_{4} \mathrm{O}_{5}(\mathrm{O})_{4}$ group in anhydrous diborates. Too few structures are yet known to guide an empirical approach. Moreover the energy associated with a change to the structure type of the strontium compound is probably quite small, so that several factors may come into play. Further structure studies in this field are thus needed before empirical rules for the boron coordination behaviour can be given.

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